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## Intermediate Division

Questions 1 to 10, 3 marks each

1.	What is the (A) 320	value of 20 × 16? (B) 140	(C) 2016	(D) 32	(E) 800	
2.	In the figure, the shaded region is what fraction of the circle? $\frac{1}{2}$					
	(A) $\frac{1}{20}$	(B) $\frac{1}{10}$	(C)	$\frac{1}{2}$ $2$	1	
	(	(D) $\frac{1}{60}$	(E) $\frac{1}{40}$	$\frac{1}{4}$	$\frac{1}{5}$	
3.	The cycling road race through the Adelaide Hills started at 11:15 am and the winner finished at 2:09 pm the same day. The winner's time in minutes was					
	(A) 135	(B) 174	(C) 164	(D) 294	(E) 186	
4.	The fraction $\frac{720163}{2016}$ is					
	(A) between	0  and  1  (B)	between 1 and 10	(C) betwee	en 10 and 100	
	(I	D) between $100$ and $1$	1000	(E) greater than 10	000	
5.	What is the value of $(1 \div 2) \div (3 \div 4)$ ?					
	(A) $\frac{2}{3}$	(B) $\frac{3}{2}$	(C) $\frac{3}{8}$	(D) $\frac{1}{6}$	(E) $\frac{1}{24}$	
6.	0.75% of a number is 6. The number is					
	(A) 800	(B) 300	(C) 1200	(D) 400	(E) 100	
7.	In the expression below, the letters $A, B, C, D$ and $E$ represent the numbers $1, 2, 3, 4$ and 5 in some order.					
	$A \times B + C \times D + E$					
	What is the largest possible value of the expression?					
	(A) 24	(B) 27	(C) 26	(D) 51	(E) 25	

8. In each of these squares, the marked length is 1 unit. Which of the squares would have the greatest perimeter?



9. On a clock face, a line is drawn between 9 and 3 and another between 12 and 8. What is the acute angle between these lines?
(A) 45°
(B) 60°
(C) 50°





10. There are 3 blue pens, 4 red pens and 5 yellow pens in a box. Without looking, I take pens from the box one by one. How many pens do I need to take from the box to be certain that I have at least one pen of each colour?

E) 12
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- **13.** A circle of radius 1 metre is inscribed inside a semicircle of radius 2 metres. What is the area in square metres of the semicircle *not* covered by the circle? (A)  $2\pi$ (C) 2 (B)  $\pi - 1$ (D)  $2\pi - 1$ (E)  $\pi$ 14. The value of n for which  $4^{n+1} = 2^{10}$  is (A) 9 (B) 8(C) 4(E) 2(D) 10 **15.** Adrienne, Betty and Cathy were the only three competitors participating in a series of athletic events. In each event, the winner gets 3 points, second gets 2 points and third gets 1 point. After the events, Adrienne has 8 points, Betty has 11 points and Cathy has 5 points. In how many events did Adrienne come second? (A) 0(D) 3 (B) 1(C) 2(E) 4
- 16. What is the smallest number N for which  $\frac{2016}{N}$  is a perfect square? (A) 14 (B) 2 (C) 56 (D) 12 (E) 7
- 17. Five people are sitting around a circle. Some always tell the truth, whilst the others always lie. Each person claims to be sitting between two liars. How many of them are telling the truth?
  - (A) 0 (B) 1 (C) 2 (D) 3 (E) 4



19. Ten students sit a test consisting of 20 questions. Two students get 8 questions correct and one student gets 9 questions correct. The remaining seven students all get at least 10 questions correct and the average number of questions answered correctly by these seven students is an integer. If the average number of questions answered correctly by all ten students is also an integer, then that integer is

(A) 10	(B) 11	(C) 12	(D) 13	(E) 14
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I 3

20. This pedal-powered water pump is made from bicycle parts.
A 30-tooth gear on the pedals has a chain to a 15-tooth gear. On the same axle as the 15-tooth gear is a 32-tooth gear that drives a chain to a 40-tooth gear on the pump. For every 100 complete revolutions of the pedals, how many times does the gear on the pump turn?
(A) 160 (B) 250 (C) 107 (D) 93 (E) 37<sup>1</sup>/<sub>2</sub>

## Questions 21 to 25, 5 marks each

21. A gardener wishes to put a circular water feature (pool) in a right-angled triangular plot that has sides of 6 m and 8 m on its two smallest sides. What is the radius in metres of the largest pool that will fit?



- (A)  $2\sqrt{2} 1$  (B) 2 (C) 4 (D) 3 (E)  $2\sqrt{2}$
- 22. A sequence of 10 letters is made according to the following rules.
  - The letter P can only be followed by Q or R.
  - The letter Q can only be followed by R or S.
  - The letter R can only be followed by S or T.
  - The letter S can only be followed by T or P.
  - The letter T can only be followed by P or Q.

How many possible sequences are there where the first, fourth, and tenth letters are all Q?

(A) 63  (H)	3) 39 (	(C) 32	(D) 45	(E) 36
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23. Cynthia's afternoon train normally arrives at her station at 5:30 pm each day, where she is picked up by Alan and driven home.

One day she was on an earlier train which arrived at 5 pm, and she decided to walk in the direction Alan was coming from home. Alan had left in time to meet the 5:30 pm train, but this time he picked up Cynthia and they arrived home 10 minutes earlier than usual.

For how many minutes had Cynthia walked before Alan picked her up?

(A) 20 (B) 30 (C) 25 (D) 10 (E) 15

I 4

- 24. You have an unlimited supply of five different coloured pop-sticks, and want to make as many different coloured equilateral triangles as possible, using three sticks. One example is shown here. Two triangles are not considered different if they are rotations or reflections of each other. How many different triangles are possible?
  (A) 35 (B) 5 (C) 20 (D) 56 (E) 10
- **25.** A *super-Fibonacci* sequence is a list of whole numbers with the property that, from the third term onwards, every term is the sum of all of the previous terms. For example,
  - $1, 4, 5, 10, \ldots$

How many super-Fibonacci sequences starting with 1 involve the number 2016?

(A) 1	(B) $3$	(C) 5	(D) $7$	(E) 9
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For questions 26 to 30, shade the answer as an integer from 0 to 999 in the space provided on the answer sheet.

Question 26 is 6 marks, question 27 is 7 marks, question 28 is 8 marks, question 29 is 9 marks and question 30 is 10 marks.

26. The right-angled triangle ABC has area 2016 cm<sup>2</sup>. Lines AI, IF, IE, EH, HD, DG divide the large triangle into seven smaller triangles of equal area. If △BIE is an isosceles triangle, find the length of BG in centimetres.



I 5

27. A symmetrical cross with equal arms has an area of 2016 cm<sup>2</sup> and all sides of integer length in centimetres. What is the smallest perimeter the cross can have, in centimetres?



28. The ten students in Malcolm's maths class all took a test. The scores of the other nine students were 82, 83, 85, 89, 90, 92, 95, 97, and 98, and Malcolm's score was a whole number.

The teacher had made a mistake in calculating Malcolm's score. After she corrected her mistake, both the mean and the median of all the scores increased by 0.5.

There are two possible correct scores that Malcolm could have had. What is the sum of these two scores?

- 29. A high school marching band can be arranged in a rectangular formation with exactly three boys in each row and exactly five girls in each column. There are several sizes of marching band for which this is possible. What is the sum of all such possible sizes?
- **30.** Around a circle, I place 64 equally spaced points, so that there are  $64 \times 63 \div 2 = 2016$  possible chords between these points.

I draw some of these chords, but each chord cannot cut across more than one other chord.

What is the maximum number of chords I can draw?

