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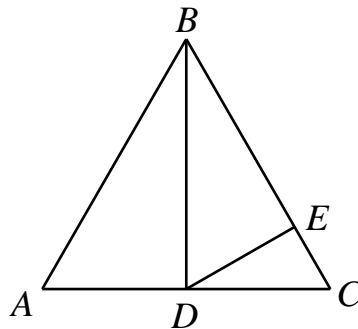
2014 Taiwan Selection Test for PMWC and EMIC

Final Round Paper I (Time Allowed : 90 Minutes)

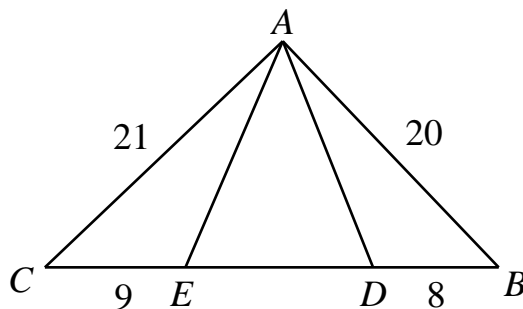
● Write down all answers on the answer sheet.

Each problem is worth 10 points and the total is 120 points.

1. Going at the average speed of 40 km per hour, we will be 1 hour late. Going at the average speed of 60 km per hour, we will be 1 hour early. At what average speed, in km per hour, should we go in order to arrive just in time?
2. ABC is an equilateral triangle of side length 4 cm. D is a point on AC such that BD is perpendicular to AC , and E is a point on CB such that DE is perpendicular to CB . What is the area, in cm^2 , of a square whose side length is DE ?

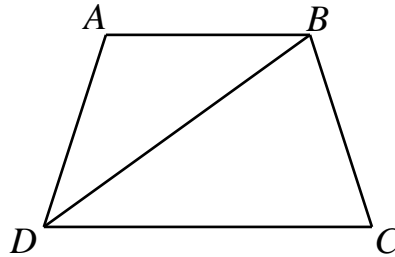


3. Trains go from town A to town B at regular intervals, all travelling at the same constant speed. A train going from town B to town A at the same constant speed along a parallel track meets the trains going in the opposite direction every 10 minutes. How often, in minutes, do the trains go from town A to town B?
4. In triangle ABC , $BC = 29$ cm, $CA = 21$ cm and $AB = 20$ cm. D and E are points on BC such that $BD = 8$ cm and $CE = 9$ cm. Determine the measure, in degrees, of $\angle EAD$.



5. What is the largest possible remainder when a two-digit number is divided by the sum of its digits?

6. In the quadrilateral $ABCD$, AB is parallel to DC , $AB < DC$ and $AD = BC$. The diagonal BD divides $ABCD$ into two isosceles triangles. Determine the measure, in degrees, of $\angle C$.



7. Every two of A, B and C play one game against each other, scoring 2 points for a win, 1 point for a draw and 0 points for a loss. How many different pairs of numbers are there such that the first is A's total score and the second is B's total score?
8. Find the sum of all positive integers less than 100, each of which has exactly 10 positive divisors.
9. The minute hand of a clock is moving as though it is the hour hand, while the hour hand is moving as though it is the minute hand. At six o'clock in the evening, the clock is showing the correct time. Next day, shortly after seven o'clock in the morning, it shows the correct time again. How many minutes after seven o'clock does that happen?
10. The first three digits of a common multiple of 7, 8 and 9 form the number 523. What is the maximum value of the number formed from its last three digits?
11. Among the positive integers between 1000 and 10000, how many multiples of 9 are there such that the sum of the first two digits is equal to the sum of the last two digits?
12. The numbers 1, 2, . . . , 25 are to be placed in a 5×5 table, with one number exactly in each square. Consecutive numbers occupy squares with a common side. Three of the numbers have been placed, as shown in the diagram below. Find the number of different placements of the other 22 numbers.

19		13		
		1		

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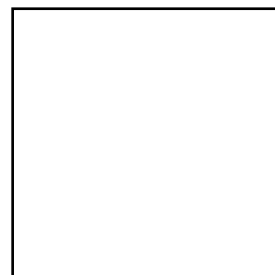
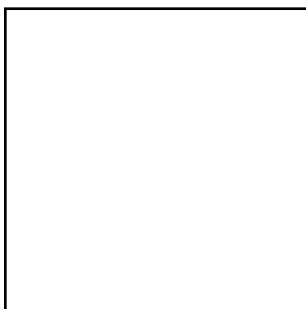
Final Round Paper II (Time Allowed : 60 Minutes)

- Complete solutions of problem 1 and 3 are required for full credits. Partial credits may be awarded. Only answers are required for problem number 2 and 4. Each problem is worth 25 points and the total is 100 points.

1. Insert three plus or minus signs between the digits of 123456789 so that the value of the resulting expression is 100.

Answer : 1 2 3 4 5 6 7 8 9 = 100

2. What is the minimum number of obtuse triangles into which a square may be dissected?



Answer : _____

